

# Magnetotransport in Single Crystal Half-Heusler Compounds

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## Abstract

We present the results of electrical resistivity and Hall effect measurements on single crystals of HfNiSn, TiPtSn, and TiNiSn. Semiconducting behavior is observed in each case, involving the transport of a small number of highly compensated carriers. Magnetization measurements suggest that impurities and site disorder create both localized magnetic moments and extended paramagnetic states, with the susceptibility of the latter increasing strongly with reduced temperature. The magnetoresistance is sublinear or linear in fields ranging from 0.01 - 9 Tesla at the lowest temperatures. As the temperature increases, the normal quadratic magnetoresistance is regained, initially at low fields, and at the highest temperatures extending over the complete range of fields. The origin of the vanishingly small field scale implied by these measurements remains unknown, presenting a challenge to existing classical and quantum mechanical theories of magnetoresistance.

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One of the most exotic settings for small gap insulators is among materials made entirely of metals, i.e. intermetallic compounds. Nonetheless, it was demonstrated in the early 1990's that a subset of the half-Heusler compounds, with the generic formula  $RNX$  ( $R, N$  are transition metal elements, and  $X$  is a main group element), display semiconducting transport while infrared absorption experiments found semiconducting gaps with magnitudes of  $\sim 100$  meV or less [1, 2]. In subsequent years, these materials were found to have a substantial thermopower [2, 3], and a number of different compositions were explored [4, 5, 6, 7, 8] in the hopes of optimizing these characteristics. All of these experiments were carried out on polycrystalline samples, and since annealing dramatically affected their transport properties [2, 4], it was clear that the samples were unlikely to be either stoichiometric, or single phase. Understanding the intrinsic behaviors of these unusual materials has awaited the synthesis of single crystal samples, which we report here.

Many intermetallic compounds form in the Heusler structure  $RN_2X$ , with four interpenetrating face centered cubic lattices, where the  $N$  elements lie at the center of the rock-salt cube formed by the  $R$  and  $X$  elements. The half-Heuslers are a variant on this structure, where one of the sublattices is entirely vacant, implying that now the  $N$  atoms ideally occupy every other rock-salt cube. This  $MgAgAs$  structure is found in intermetallic compounds with 16-20 electrons per formula unit  $z$ , but most often when  $z=18$  as in the  $RNiSn$  ( $R=Ti, Zr$ , and  $Hf$ ) [9]. Of the known half-Heusler compounds [10], only a few are thought to be insulating in the absence of disorder:  $RNiSn$  ( $R=Ti, Zr$ , and  $Hf$ ) and  $RNSn$  ( $R=Zr$  and  $Hf$ ,  $N=Pd$  and  $Pt$ ) [1],  $LnPdSb$  ( $Ln=Ho, Er, Dy$ ) [6],  $LnPtSb$  ( $Ln=$ trivalent rare earth) [8],  $CoTiSb$  and  $CoNbSn$  [7], and  $NbIrSn$  [5]. Studies of half-Heusler systems in which the electron count is changed systematically [7, 11, 12] reveal that insulating behavior is generally observed near  $z=18$ , while metallic and sometimes magnetically ordered systems are found at both higher and lower electron counts. We note that this result is based largely on resistance measurements carried out on polycrystalline samples, and that site disorder is potentially large in the half-Heusler structure, even for nominally stoichiometric compositions [1, 4]. For these reasons, the exact range of intrinsic insulating behavior, is still experimentally uncertain. Electronic structure calculations [13] support the view that the semiconducting behavior found in the  $RNiSn$  ( $R=Ti, Zr, Hf$ ) is an intrinsic feature, finding indirect gaps between the  $\Gamma$  and  $X$  points in each compound. The gap is determined by the strength of the  $R$ - $Sn$   $pd$  hybridization, which leads to anticrossing of the extrema of the conduction and

valence bands, which have primarily R  $d_{xy}$  character. The anticrossing is further amplified through an indirect interaction of the R states mediated by low lying Ni states. Nonetheless, the indirect gaps in TiNiSn, ZrNiSn, and HfNiSn are expected to be nearly identical,  $\sim 0.5$  eV.

The purposes of this paper are two fold. First, we report the results of transport and magnetization experiments on single crystals of TiNiSn, HfNiSn, and TiPtSn. For comparison, similar experiments were carried out on polycrystalline samples as well. These measurements show that the semiconducting behavior found in polycrystalline samples is at least partly intrinsic, although electron microscopy evidence is presented which reveals substantial metallurgical phase separation in all polycrystalline samples. All of the samples, both single crystal and polycrystalline, are weakly magnetic, due to the presence of both extended and localized moment bearing defect states. The Hall constant is unusually small, suggesting a near balance of electrons and holes. While our original objective was to establish the RNiSn as intrinsic semiconductors by measuring single crystals instead of polycrystals, we found in addition that the magnetotransport is anomalous in this family of compounds. The second section of this paper is devoted to a description of the linear magnetoresistance found above a field scale which grows linearly with temperature, and which varies only moderately among our different samples.

Polycrystalline samples of HfNiSn were prepared by arc melting in a high purity Ar atmosphere, followed by high temperature vacuum annealing. An electron backscattering image of the as cast material is shown in Fig. 1a, revealing that most of the sample is near-stoichiometric HfNiSn, but that there are additional phases at the boundaries of the grains. Microprobe measurements find that these phases are roughly equal quantities of  $\text{Hf}_5\text{Sn}_4$  and the Heusler compound  $\text{HfNi}_2\text{Sn}$ , together making up about 4% of the total as cast sample volume. After annealing the as cast material in vacuum at 1000 C for 720 hours [1], the grain boundary phases are much reduced in volume (Fig. 1b), and we presume that the composition of the grains approaches the stoichiometric level. Annealing had very similar effects on both TiNiSn and ZrNiSn polycrystals, which were found to undergo even more extensive phase separation. We also attempted to introduce B,Ta,Lu,Co,Mn,U,and Ce into HfNiSn and ZrNiSn as dopants. In every case, the dopants were segregated in the grain boundary phases, with no measurable solubility in the HfNiSn and ZrNiSn grains. We note that earlier efforts to dope the RNiSn also employed some of these elements [4, 10, 14],

and our results suggest that the primary effects of doping observed in these works likely result from modifications to the conducting properties of the grain boundary phases, and not from changes in the RNiSn matrix itself. We also experimented with shorter anneals at higher temperatures. Fig. 1c shows that a 72 hour anneal at 1300 C significantly decreases the volume of grain boundary phases, which is now largely  $\text{Hf}_5\text{Sn}_4$ , although higher levels of  $\text{HfNi}_2\text{Sn}$  and significant Sn loss from the matrix are observed near the surface of the polycrystalline sample. Due in part to these concerns about sample homogeneity, single crystals of HfNiSn were prepared at the University of Amsterdam/Leiden University ALMOS facility using the tri-arc assisted Czolchralski method, while single crystals of TiNiSn and TiPtSn were synthesized at Ames Laboratory from a Sn flux [15]. The crystal structures of all HfNiSn samples, both single crystal and polycrystal, were verified to be the MgAgAs type by powder x-ray diffraction.

We have studied these samples using both magnetization measurements, carried out using a Quantum Designs SQUID magnetometer, and electrical transport measurements, which employed both a Quantum Designs Physical Phenomena Measurement System and home-built helium cryostat systems. The resistivity and Hall effect measurements were performed at a frequency of 17 Hz, in the conventional four-probe and five probe configurations, respectively. Sweeps in positive and negative fields were combined to separate the mixed Hall signal and longitudinal magnetoresistance at each temperature. Special care was taken to avoid heating by the measuring current, especially at the lowest temperatures.

Sample homogeneity has a profound effect on the transport observed in the half-Heuslers. Fig. 2 depicts the temperature dependent resistivity for four different samples of HfNiSn: single crystal, as cast polycrystal, and polycrystal annealed for 720 hours at 1000C (optimally annealed), and 72 hours at 1300 C. The resistivity increases slowly with decreasing temperature in the as cast material and reaches a broad maximum near 120 K, before decreasing and displaying a superconducting transition near 3.8 K. The superconductivity is easily suppressed with modest fields, and since it is absent in the optimally annealed and single crystal samples we ascribe it to the grain boundary phases, or to trace amounts of elemental Sn. The resistivity of the optimally annealed polycrystalline sample reproduces the insulating behavior of the single crystal, although its resistivity is more than an order of magnitude smaller for the entire temperature range. The 72 hour/1300C anneal has an intermediate effect, marginally increasing the measured resistivity over that of the as-cast

sample, while rendering it insulating down to the superconducting transition. We conclude from the data in Fig. 2 that the grain boundary phases are highly conducting relative to the matrix, but that once they are removed by annealing HfNiSn is intrinsically a semiconductor, as previously claimed on the basis of experimental evidence gathered from the polycrystalline samples [1].

Despite their intermetallic character, the single crystals of HfNiSn, TiNiSn, and TiPtSn all display semiconducting behavior, as predicted for filled d-band half-Heuslers [13]. Fig. 3a shows the temperature dependences of the electrical resistivity of samples of all three materials, showing the behavior typical of n-type semiconductors. The activation plots of Fig. 3b are not linear over the entire range of temperatures investigated. In every case, the resistivity slowly approaches a constant value at the lowest temperatures, but in addition there are regions of distinctly different slopes, especially for TiNiSn. These results indicate the presence of narrow bands of impurity/defect states in the semiconducting gap, with excitation energies which are smaller than the semiconducting gap itself. The highest temperature transport gaps are very small: 26 meV for HfNiSn, 28 meV for TiPtSn, and 79 meV for TiNiSn. The estimates for the transport gaps in HfNiSn and TiNiSn are much smaller than the values previously reported for polycrystals [1], as well as being smaller than the indirect gap of 0.5 eV predicted by electronic structure calculations for TiNiSn and HfNiSn [13].

Hall effect measurements have been carried out on single crystals of HfNiSn, TiNiSn and TiPtSn, in order to estimate the number and type of carriers present. The data are presented in Fig. 4a. No Hall signal was detected in single crystal or polycrystalline HfNiSn in fields as large as 9 Tesla, and for temperatures between 1.2 K and 12 K. Our experimental accuracy consequently yields only a lower bound for a single band carrier concentration  $n$  of  $5 \times 10^{21} \text{ cm}^{-3}$ , which is more than one carrier per unit cell. The Hall constant in TiPtSn is just at the limits of our experimental resolution, and also indicates a large carrier concentration  $\sim 1 \times 10^{21} \text{ cm}^{-3}$ . In view of the semiconducting characters of single crystal HfNiSn and TiPtSn, we view these single band carrier concentrations as unreasonably high. We consider it more likely that both HfNiSn and TiPtSn are very close to perfect compensation, and perhaps may even be semimetals. In contrast, a large Hall voltage was detected in TiNiSn, linear in field and with a slope which indicates that the dominant carriers are electrons. The temperature dependence of the electron concentration  $n$  deduced from these measurements is plotted in

Fig. 4b, showing a strong increase with reduced temperature, amounting to an increase by approximately one electron per 365 unit cells between 40 K and the approximately constant value of  $1 \times 10^{19} \text{ cm}^{-3}$  found below 15 K. It is significant that the low temperature electron concentration in TiNiSn is approximately the same as the number of paramagnetic moments inferred from the magnetization measurements, which we discuss next.

All of the single crystal and polycrystalline samples we measured are weakly magnetic, despite the nominally nonmagnetic character expected for the filled-d shell half-Heusler compounds. The field dependence of the magnetization of polycrystalline HfNiSn, annealed for 720 hours at 1000 C, is presented in Fig. 5a, while similar data for single crystal TiNiSn appear in Fig. 5b. In both cases, the magnetization is strongly nonlinear, especially at low fields and low temperatures. As the temperature is raised, the magnetization is increasingly dominated by a diamagnetic contribution, linear in field, which is especially evident for the TiNiSn sample. The magnetization  $M$  divided by a constant measuring field of 1.5 T is plotted in Fig. 6 as a function of temperature for three different samples: polycrystalline HfNiSn, both as cast and annealed for 720 hours at 1000 C, as well as single crystal TiNiSn. Fig. 6 shows that the paramagnetic contribution to the magnetization is largest at low temperatures, but is superposed on a diamagnetic contribution. It is evident that the magnitudes of the paramagnetic and diamagnetic components, as well as their relative weights, vary considerably among the samples we investigated.

Figures 5 and 6 suggest that it may be possible to separate the two components of the magnetization by modelling the magnetization in each sample as  $M(H,T) = \chi_o H + \mathcal{F}(H/T)$ . The first term represents a field independent susceptibility, which we will show combines the normal diamagnetic susceptibility of the semiconducting host, with an additional Pauli paramagnetic susceptibility, which varies among samples. Given the small magnitude of the moments shown in Fig. 5, we think it unlikely that long range magnetic order is responsible for the nonlinear magnetization found at low temperatures. Instead, we suggest that the second term represents the scaling behavior of isolated and localized magnetic moments, where  $\mathcal{F}$  is consequently expected to be the Brillouin function.

The results of this modelling are shown in Fig. 7, which demonstrates that the magnetization sweeps taken in both samples for temperatures which range from 2 K - 20 K collapse onto scaling curves if a diamagnetic term is previously subtracted from the data at each temperature. As indicated, the scaled and corrected magnetizations for HfNiSN and TiNiSn

are well described by  $J=1/2$  Brillouin functions, yielding moment densities of  $1.98 \times 10^{-3} \mu_B$  per formula unit TiNiSn and  $1.55 \times 10^{-3} \mu_B$  and  $0.144 \mu_B$  per formula unit HfNiSn for the two annealed and polycrystalline HfNiSn samples investigated. We find that the diamagnetic susceptibilities  $\chi_o$  of the three systems are also very different, as Fig. 6 suggests. These susceptibilities are plotted in Fig. 8, showing that  $|\chi_o|$  is much larger for TiNiSn than for either HfNiSn sample, although  $|\chi_o|$  varies by almost an order of magnitude between the two HfNiSn samples. While  $\chi_o$  approaches a constant value at low temperature in one of the polycrystalline HfNiSn samples (filled circles), in each of the three samples,  $|\chi_o|$  increases approximately linearly with temperature.

The pronounced temperature and sample dependences of  $\chi_o$  which are demonstrated in Fig. 8 argue strongly for the presence of a paramagnetic contribution to the magnetization which is linear in field. The susceptibility of a semiconductor is approximated by the sum of the core susceptibilities of the constituent atoms:  $-4.8 \times 10^{-5}$  emu/g for HfNiSn and  $-3.7 \times 10^{-5}$  for TiNiSn[16], and is consequently independent of temperature and invariant among samples of the same nominal composition. The values we find for  $\chi_o$  in HfNiSn and TiNiSn do not approach these limits on the temperature range of our experiment, suggesting the presence of an additional positive magnetization, linear in field and decreasing in magnitude with increasing temperature. The variation of  $\chi_o$  between the two HfNiSn samples suggests that this inferred positive susceptibility has an extrinsic origin, consistent with the small magnitude of the local moments found in each sample, and with the variations in moment concentrations found among different samples.

We conclude that there are two magnetic entities present with different relative weights in each of our half-Heusler samples, superposed on the diamagnetic response of the semi-conducting host. The first entities are localized magnetic moments, perhaps generated by the inevitable site disorder characteristic of the half-Heusler structure. Still, the level of this putative disorder can be quite low, corresponding to only one defect per 7000 unit cells in our least magnetic HfNiSn sample. Secondly, we propose that there are also extended and metallic states present which are responsible for the inferred paramagnetic susceptibility. In agreement with Hall effect measurements on TiNiSn, the number of these metallic states grows with decreasing temperature. It is interesting that the electron concentration in TiNiSn is similar to the concentration of localized magnetic moments, suggestive that both have the same origin, presumably defects or impurities. Further, the data suggest that the



electron contributed by each impurity or defect in TiNiSn ultimately becomes delocalized as  $T \rightarrow 0$ , which is, intriguingly, just what is expected if the moment bearing impurities are compensated by the Kondo effect.

Perhaps the most striking property of the nonmetallic half-Heusler compounds is their magnetoresistance, which is linear or even sublinear in field at the lowest temperatures. The anomalous magnetoresistance has been observed in every half-Heusler compound we have measured, both single crystals and polycrystals, both as cast and annealed. This is demonstrated in Fig. 9 which presents the 2 K magnetoresistances of HfNiSn, TiPtSn, and TiNiSn single crystals, and HfNiSn polycrystal, both as cast and annealed for 720 hours at 1000C. The magnetoresistances of the single crystal samples are markedly sublinear, while those of the polycrystalline samples are more highly linear. In neither case is there any suggestion of a quadratic magnetoresistance, down to fields as small as 1000 Oe. We note that trace superconductivity in the polycrystalline samples prohibits measurements to fields less than  $\sim 500$  Oe. The magnitude of the magnetoresistance is rather modest, amounting to a few percent in each of the crystalline samples. It approaches 10% at 9 T in the as-cast polycrystalline sample, although annealing reduces the magnetoresistance to the level observed in the single crystals. This may result either from a compactification of the internal structure of the polycrystals, since annealing removes conducting grain boundaries, or from rendering the HfNiSn grains more nearly stoichiometric, as in the single crystal.

The low field magnetoresistance of all samples ultimately becomes quadratic in field if the temperature is increased sufficiently. The longitudinal magnetoresistance of single crystal HfNiSn is presented at several temperatures in Fig. 10, with an expanded low field region in the inset. At 2 K, the magnetoresistance is sublinear over our entire field range, and is never quadratic, even at the lowest fields. At 4 K, the magnetoresistance is linear over virtually the entire range of fields studied, with little trace of the upward curvature which emerges at the lowest fields at 6 K. Raising the temperature still further yields a range of fields for which quadratic magnetoresistance is found. This is demonstrated in Fig. 11, where the magnetoresistance of single crystal HfNiSn is plotted as a function of  $H^2$ . At 30 K and above, the magnetoresistance is quadratic in field for the entire range of fields studied, 0.01 -9 T. As the temperature is lowered, clear departures from  $\Delta\rho/\rho \propto H^2$  are observed, below fields  $H^*$  which become progressively smaller as the temperature is reduced. This analysis has been repeated on all of our samples, and the results are summarized in Fig. 12. It is evident

that the range of fields  $H \leq H^*$  and temperatures for which  $\Delta\rho/\rho \propto H^2$  varies considerably among the different samples. For instance, the magnetoresistance of the annealed sample of HfNiSn (open circles, Fig. 12) is quadratic in fields up to 9 T for all temperatures above 15 K, while clear departures are still evident at temperatures as large as 100 K for an as cast polycrystalline sample of HfNiSn (open squares, Fig. 12).

Fig. 12 may be viewed as an organizational scheme for our magnetoresistance observations, analogous to a phase diagram, where  $H^*(T)$  represents a crossover from a regime at low fields where the magnetoresistance is quadratic in field, to a regime at high fields where the magnetoresistance is linear or even sublinear in field. In agreement with the discussion of Fig. 9, the linear magnetoresistance is seen for the widest range of temperatures in the as cast polycrystalline samples, while annealing confines the linear magnetoresistance to the lowest temperatures and highest fields.  $H^*(T)$  for the single crystals is similar to that of the most homogeneous polycrystalline samples, which have been annealed for the longest times.

The observation of a linear or sublinear magnetoresistance is anomalous, as the magnetoresistance typically depends on the field magnitude, yielding a magnetoresistance which is even and usually quadratic in the applied field. Nonetheless, there are a few circumstances in which a linear magnetoresistance is expected. A linear magnetoresistance can occur in inhomogeneous materials, resulting from the accidental admixture of the Hall signal[17]. We rule out this possibility for the half-Heuslers, as we observe linear magnetoresistance in single crystals, and further since the Hall signal is immeasurably small, especially in HfNiSn and TiPtSn. Similarly, a variety of different mechanisms can lead to linear magnetoresistance in systems with large carrier concentrations[18, 19], but in most cases their application to the minimally magnetic and essentially semiconducting half-Heuslers seems tenuous. Finally, we note that there is no evidence for either magnetic or structural transitions, which might provide an internal symmetry breaking field, superseding the applied field.

Linear magnetoresistance is expected in metals with closed Fermi surface orbits at intermediate fields, in a crossover regime between the quadratic magnetoresistance expected at low fields, and saturation at high fields. The range of fields over which linear magnetoresistance can be observed is potentially quite extensive for materials with a high degree of compensation [? ]. However, this linear crossover regime emerges when the product of the cyclotron frequency  $\omega_c$  and the scattering time  $\tau$  exceeds one,  $\omega_c\tau \geq 1$ . For TiNiSn at 2 K, where  $n=1.3 \times 10^{19}$  and  $\rho=18 \Omega\text{-cm}$ ,  $\omega_c\tau=1$  for an applied field of  $3.7 \times 10^5$  Tesla. Indeed,

this crossover field could be considerably larger if we consider that the Hall measurements provide only a lower bound on the total number of carriers, which may be electrons as well as holes. Conversely, if we assume that this crossover field is no more than 100 Oe, consistent with our lowest temperature magnetoresistance results on single crystal HfNiSn and TiPtSn, we would require a total carrier concentration of  $\sim 3 \times 10^{13} \text{ cm}^{-3}$ . It is difficult to believe that the numbers of electrons and holes present in both our single crystal and polycrystalline samples are balanced at the level of one carrier per  $10^8$  unit cells, as the absence of a Hall signal suggests. We are forced to conclude that in each of our samples, linear or sublinear magnetoresistance is observed for a wide range of fields which are comfortably in the low field limit  $\omega_c \tau \ll 1$ .

Linear magnetoresistance is also predicted theoretically for a low density electron gas, in which only the lowest Landau level is occupied [21, 22, 23]. The two requirements for realizing this quantum magnetoresistance are that  $H \geq (\hbar c n)^{2/3}$ , and that  $T \ll e H \hbar / m^* c$ . Consequently, the linear magnetoresistance should only be observed in TiNiSn at fields greater than 36 Tesla, and for temperatures  $T \ll 1.35 \text{ (K/T)H}$ . It is possible that the latter condition is satisfied in the half-Heusler compounds, since as Fig. 11 demonstrates, the linear magnetoresistance is only observed above a field  $H^*$  which increases linearly with temperature. In this view, the different slopes found in the plot of  $H^*(T)$  for the different systems (Fig. 11) could plausibly be the result of variations in magnitude of the effective mass between the least massive ( $m^*/m=0.09$  in as cast HfNiSn 99106) and the heaviest ( $m^*/m=0.58$  in single crystal TiPtSn). Nonetheless, our observation of linear magnetoresistance in TiNiSn in fields as small as 0.01 T, where the criterion  $H \geq (\hbar c n)^{2/3}$  is dramatically violated is problematic for the quantum magnetoresistance theory as well. One possibility is that only a tiny fraction of the carriers detected by the Hall effect in TiNiSn, one carrier in  $\sim 2 \times 10^5$ , actually participates in the quantum magnetoresistance. We note that a similar explanation has been proposed [22] as an explanation for the linear magnetoresistance observed in doped silver chalcogenide compounds [24, 25, 26, 27]. Here, spatial separation of conducting and insulating regions was invoked to achieve the needed reduction in effective carrier concentration, a scenario which is inapplicable to the single crystal half-Heuslers. The central dilemma lies with explaining the unexpected persistence of the linear and sublinear magnetoresistance to extremely low fields, particularly at low temperatures. If the linear magnetoresistance observed in the half-Heuslers derives from the scattering of fully quantum mechanical states,

then our measurements suggest a less restrictive set of necessary conditions than has been theoretically proposed.

It is unclear whether the linear magnetoresistances found in the half-Heuslers and the silver chalcogenides arise from the same fundamental mechanism. Certainly there are general resemblances between the doped silver chalcogenides and the semiconducting half-Heuslers, as both systems are nonmagnetic semiconductors, with small or vanishing values of the Hall constant. We note that the single crystal half-Heuslers generally have larger resistivities, and as far as is known, electron concentrations which are similar to those in optimally doped  $\text{Ag}_{2-\delta}\text{Te}$ [25]. The progression of the magnetoresistance from sublinear, to linear, and ultimately to quadratic field dependencies is achieved by increasing temperature and consequently decreasing electron concentration in the half-Heuslers. In contrast, temperature has a very modest effect on the linear magnetoresistance found in the doped silver chalcogenides[26], although the same progression of field dependencies is achieved in this system by using high pressures to drive the Hall constant through zero[25]. A similar sensitivity to carrier density is apparently absent in the half-Heuslers, since the magnetoresistances of single crystal  $\text{HfNiSn}$ ,  $\text{TiPtSn}$ , and  $\text{TiNiSn}$  are very similar in magnitude, despite their very different electron concentrations. Finally, we note that the magnetoresistances of the single crystal half-Heuslers are also much smaller than those of the silver chalcogenides, and the uniformly larger magnetoresistance found in as-cast polycrystalline half-Heusler samples may support the suggestion that compositional inhomogeneities, present only in the polycrystalline half-Heusler samples, are required to obtain large, linear magnetoresistances[22, 25].

We have established here that single crystals of several half-Heusler compounds, selected to have a total of 18 valence electrons, are small gap insulators, in agreement with both electronic structure calculations and previous measurements on polycrystalline samples. Resistivity measurements show that  $\text{HfNiSn}$ ,  $\text{TiPtSn}$ , and  $\text{TiNiSn}$  single crystals are all semiconducting, while magnetization measurements argue that both localized magnetic and extended states are introduced with impurities or site interchange disorder. Hall effect measurements indicate that the number of electrons and holes is closely balanced in  $\text{HfNiSn}$  and  $\text{TiPtSn}$ , although there is a pronounced excess of electrons in  $\text{TiNiSn}$ . Both the corresponding electron concentration and the inferred Pauli susceptibility in  $\text{TiNiSn}$  increase with decreasing temperature, which may signal the return via the Kondo effect of electrons to the Fermi surface which were formerly localized at high temperatures in magnetic impurity

states.

Our results deepen the mystery surrounding the origin of linear magnetoresistance in materials with small carrier densities. Neither the classical nor quantum mechanical theories of the magnetoresistance can countenance the persistence of the linear magnetoresistance to fields as low as 0.01 T, given the mobility and carrier densities characteristic of both half-Heuslers and the doped silver chalcogenides. The observation of the linear magnetoresistance in single crystals of the half-Heuslers, which are presumed to be compositionally homogeneous on the shortest length scales, removes a degree of freedom present in the doped silver chalcogenides. Barring another mechanism which dramatically limits the number of electrons responsible for the linear magnetoresistance in the half-Heuslers, a new explanation for the origin of the miniscule field scale in these unusual materials must be sought.

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FIG. 1: Electron backscattering images of as cast polycrystalline HfNiSn(a), and after annealing for 720 hours at 1000C (b) and for 72 hours at 1300 C(c). The white lines in each panel indicate a length of 100 microns.

FIG. 3: (a): Temperature dependent resistivities of single crystal TiPtSn (filled circles), TiNiSn (stars), and HfNiSn (filled diamonds). (b) Activation plots for the same data. Dashed lines are activation fits over the indicated temperature ranges.

FIG. 4: (a): Hall constants  $R_H$  and (b) the corresponding single band electron concentrations  $n$  for TiNiSn and TiPtSn single crystals. Solid lines indicate upper limit for  $R_H$  and lower limit for  $n$  for single crystal HfNiSn.

FIG. 5: (a) Magnetization  $M(H)$  of a HfNiSn polycrystal annealed at 1000C for 720 hours, and a TiNiSn single crystal (b). Note the large diamagnetic magnetization in (b), and the relatively much smaller diamagnetic contribution in (a), evident only in the 2 K  $M(H)$  curve above 3 T.

FIG. 6: Temperature dependence of the magnetization  $M$  divided by a 1.5 Tesla measuring field  $H$  for polycrystalline HfNiSn, both as cast and annealed for 720 hours at 1000 C, and for a single crystal of TiNiSn.

FIG. 7: Magnetization sweeps, corrected for a linear diamagnetic susceptibility, collapse onto scaling curves as a function of  $g\mu_B H/k_B T$ , for both polycrystalline HfNiSn (annealed at 1000 C for 720 hours) and single crystal TiNiSn. The solid lines are  $J=1/2$  Brillouin functions.

FIG. 8: (a): The temperature dependence of the diamagnetic susceptibility  $\chi_o$  for annealed samples of polycrystalline HfNiSn (filled circles and open squares) and single crystal TiNiSn (open circles) Solid lines are power law fits, demonstrated in a double logarithmic plot in (b). The slopes of the power law fits to  $|\chi_o|$  are 1.0 for one HfNiSn (filled circles) and TiNiSn, and 1.8 for the other HfNiSn polycrystalline sample (open squares).

FIG. 2: The temperature dependent resistivity  $\rho$  for as cast polycrystalline HfNiSn (filled circles), annealed polycrystalline HfNiSn (open circles: 720 hours at 1000 C; open squares: 72 hours at 1300 C), and for a single crystal of HfNiSn (filled squares). Note that the resistivity of the HfNiSn single crystal has been divided by 25 for comparison to the polycrystalline samples.



FIG. 9: The magnetoresistances of single crystals of HfNiSn(HfNiSn(3)), TiPtSn, and TiNiSn at 2 K. For comparison, data are shown for polycrystalline samples of HfNiSn, both as-cast (HfNiSn(1)) and annealed for 720 hours at 1000 C (HfNiSn(2)). The TiNiSn ,TiPtSn, and polycrystalline HfNiSn data have all been offset for comparison.

FIG. 10: The magnetoresistance  $\Delta\rho/\rho$  for single crystal HfNiSn at different fixed temperatures. Inset shows the same data for an expanded range of low fields. The 2 K and 4 K data in the inset have been offset vertically for comparison.

FIG. 11: The magnetoresistance of a single crystal of HfNiSn plotted as a function of the field squared at different temperatures. Vertical arrows indicate the highest field  $H^*$  at which quadratic field dependences are observed, and the dashed lines are linear fits to the data having  $H \leq H^*$ .

FIG. 12:  $H^*(T)$  defines a crossover from quadratic magnetoresistances at low fields to linear or sublinear magnetoresistance at high fields.  $H^*$  varies substantially among the different samples: Single crystal HfNiSn (filled circles), two different annealed polycrystalline HfNiSn samples (open circles, filled squares), and the corresponding two different as cast polycrystalline HfNiSn ( filled diamonds:,open squares), and single crystals of TiNiSn (filled triangles) and TiPtSn (open triangles).

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